

# ***AGLeD***

## **Advanced GRIN Lens Design for mm-wave Radiometer Systems**

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# AGLeD Introduction

- AGLeD is a Seedcorn Project to investigate the methodology in the design of a Metamaterial GRIN Lens for mm-wave radiometer systems
  - Work follows on from the CEOI Metamaterial Study 2011-2012
  - Application to Eumetsat MetOp MWS Radiometer
  
- Key objectives
  - Develop the design methodology for metamaterial lenses
  - Manufacture and Test of a trial metamaterial lens (change from original proposal)
  
- Project partners
  - **Astrium Ltd, Portsmouth**
    - Dr Graham Maxwell-Cox      Project Management and Quasi-Optical Design
    - Dr Michael Notter              Metamaterial Lens design
  - **STFC – RAL**
    - Dr Manju Henry and Anup Mistry      MM-wave Test Facilities

# Technical Report on work

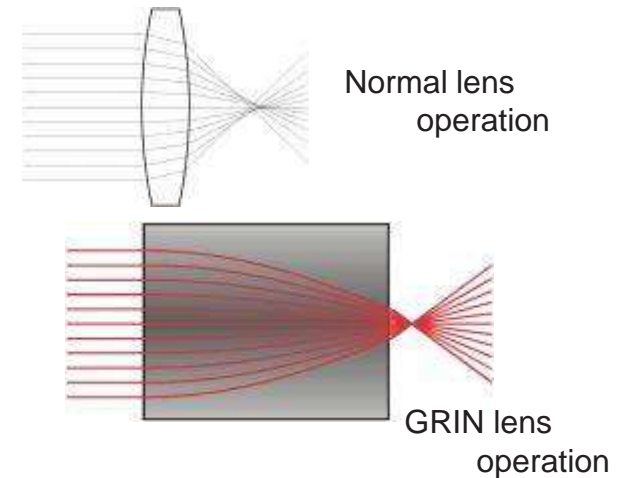
- **Dr Mike Notter Presents:**
- Some details of Advanced Gradient Index Lens (AGLeD) using metamaterials
  - Methodology
  - Design of lens
  - Lens construction
  - QO Testing

## CYLINDRICAL GRIN LENS CONSTRUCTION

- Refractive index varies radially from optical axis
- Can be made in the form of a uniaxially anisotropic medium using stacked dielectric layers with metallic loading. Each layer is usually identical. The number of layers determines the focal length

## POTENTIAL BENEFITS OFFERED :

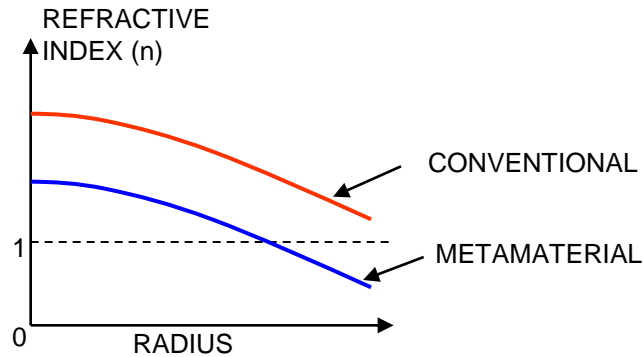
- Performance is largely unaffected by the (external) dielectric medium in which the lens operates
- Lens focal length can be changed (for a given design) by extending or reducing the length of the lens.
- Designer has greater control over ray trajectory within the body of the lens and can minimise aberrations for a given function
- Flat front and rear surfaces make the attachment or modification of matching layers straightforward
- Surface accuracy is less important than in a conventional lens.



### APPLICATIONS

- Quasi-optical beam waveguide (e.g. as in MWS).
- Millimetre-wave antenna

# NEW LENS DESIGN APPROACH USING 'METAMATERIALS'



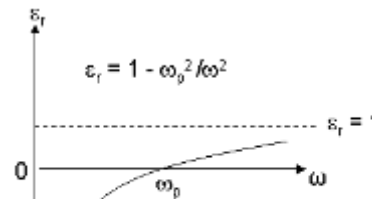
$$\text{Refractive index} = n = \sqrt{\epsilon_r \mu_r}$$

- $\mu_r$  is fixed at around unity in practice, so only  $\epsilon_r$  is varied to change 'n'
- Wave impedance =  $\sqrt{\mu_r / \epsilon_r}$

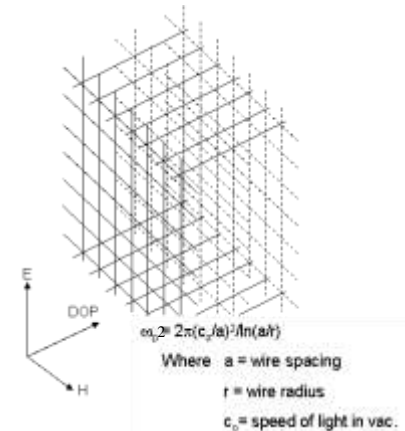
⇒ Mismatch at lens surface for  $\epsilon_r \neq 1$

**Allowing values of 'n' < 1 reduces the mismatch in wave impedances at the lens surface, and hence the reflection level.**

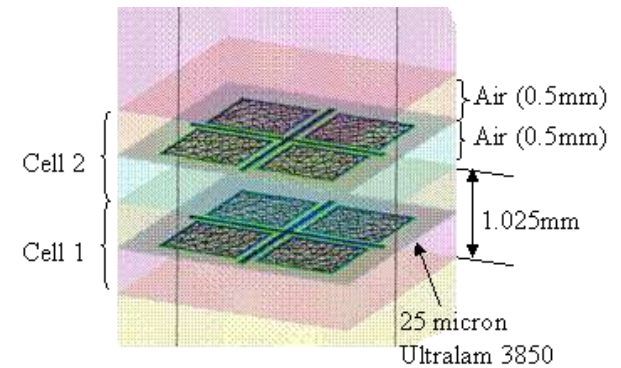
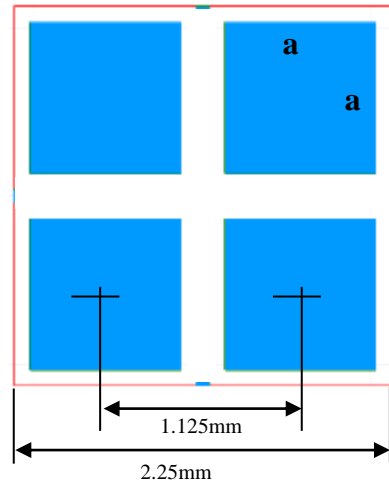
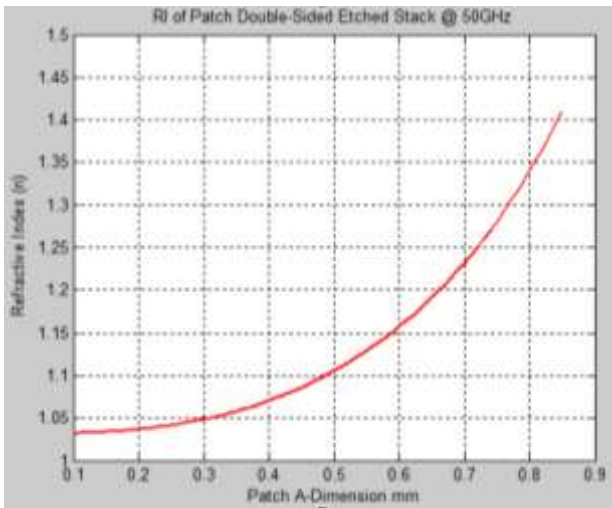
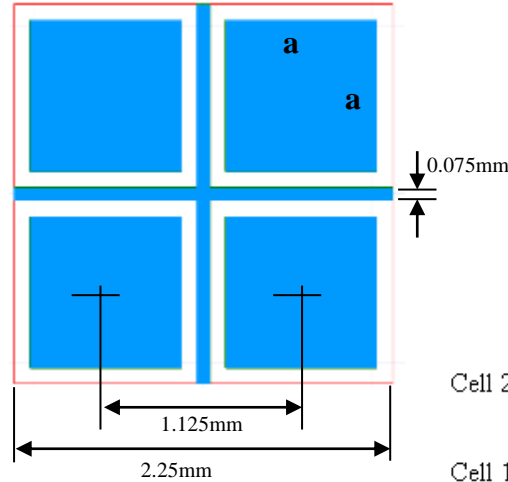
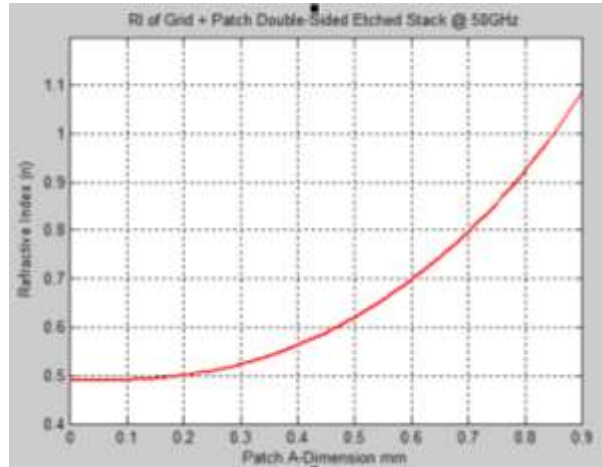
New metamaterial lens medium combines a wire grid with metal patch loading elements to provide a range of refractive index values from 0.5 to 1.4 @ 50GHz



**Wire grid response**

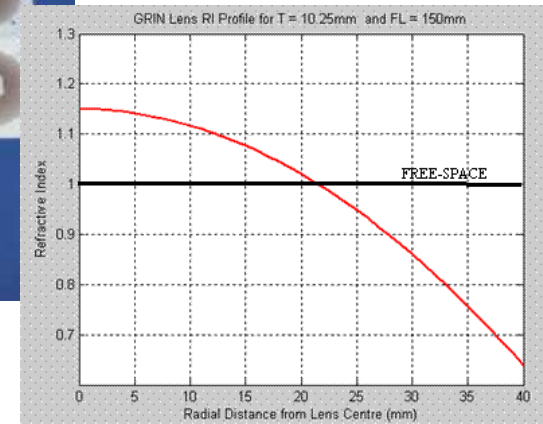
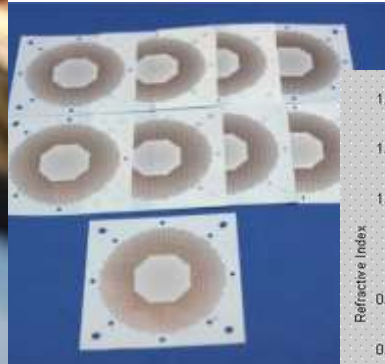
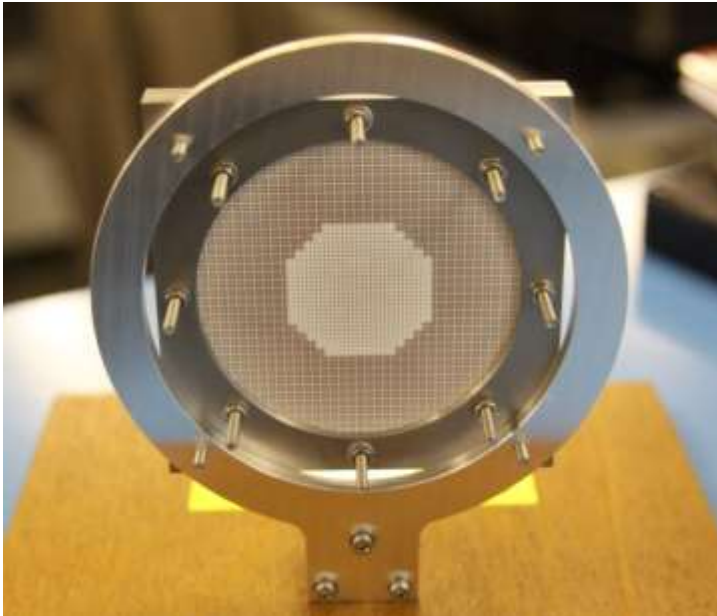


# LENS MEDIUM CONSTRUCTION AND RF PROPERTIES @ 50GHz



## Parameters:-

- Lateral cell size: 2.25mm x 2.25mm
- Substrate: 25micron Ultralam 3850
- Substrate spacing: 1.025mm (= vertical cell size)
- Double-sided (0.5 oz) copper trace
- 50GHz design frequency



REQUIRED REFRACTIVE INDEX  
PROFILE

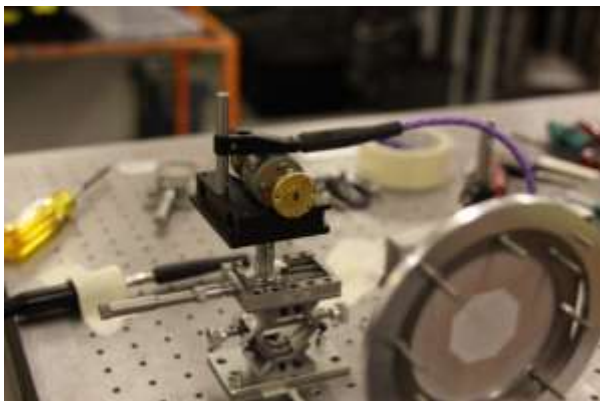
## LENS DESIGN PARAMETERS

- Diameter: 80mm
- Number of layers: 10-off (9-off in practice)
- Focal length: 150mm (166mm with 9 layers)
- Design Frequency: 50GHz

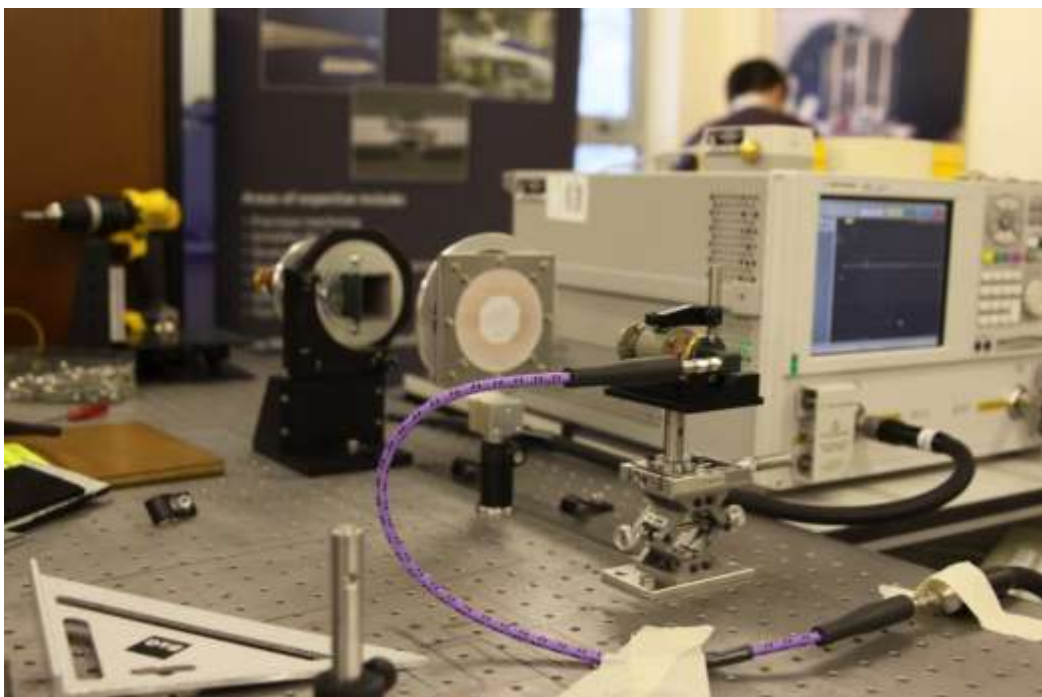
Expected beam waist diameters at 50GHz:-

- 27.5mm for uniform lens illumination
- 36.7mm for  $(1-r^2)$  amplitude taper across lens

# Test Setup



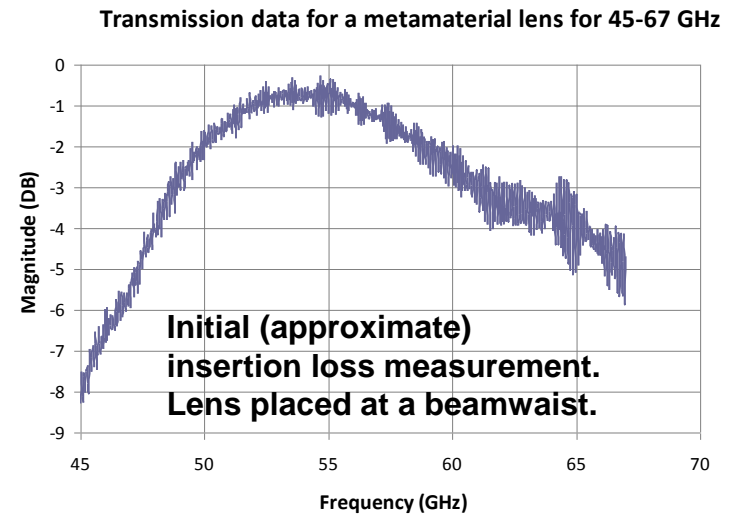
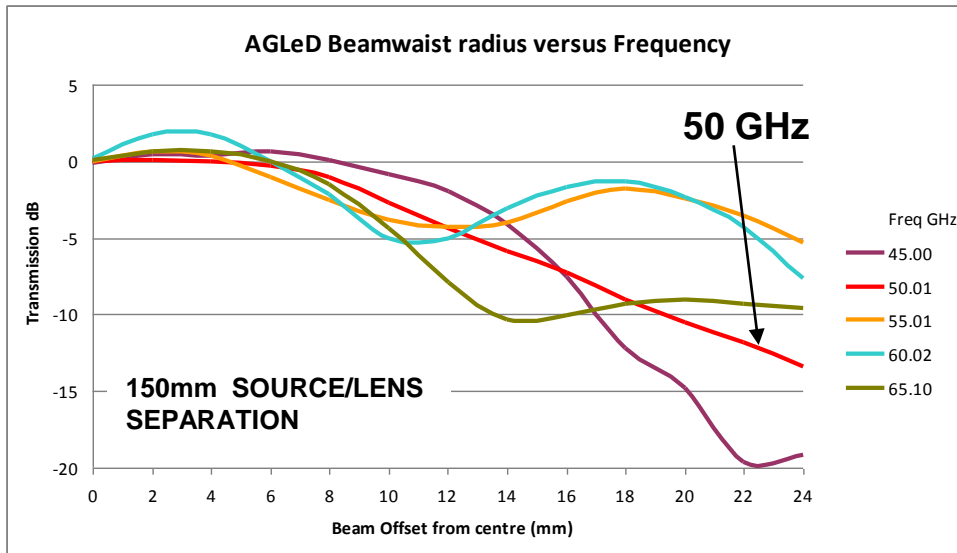
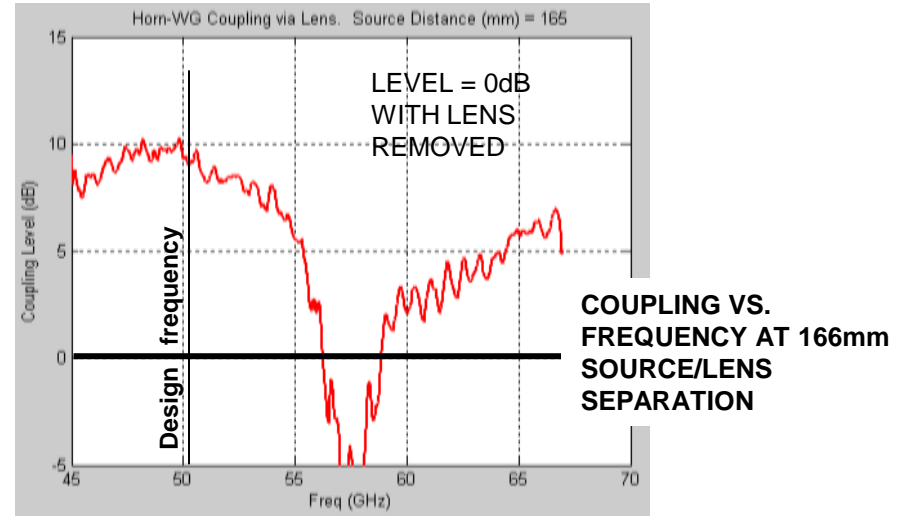
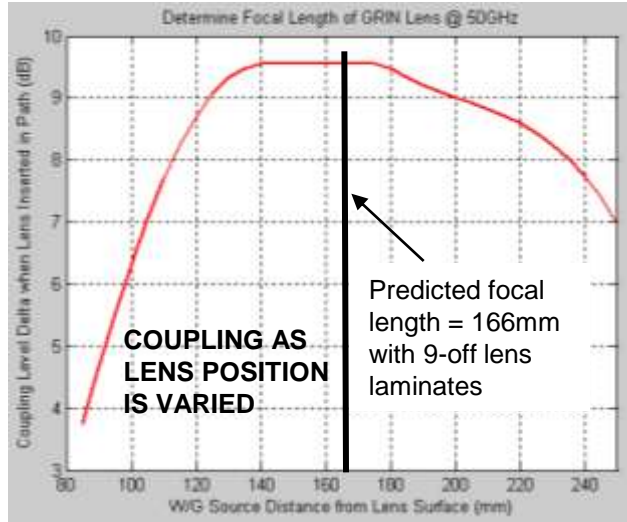
Source orientation to maximise measurement resolution and to minimise spurious illumination of table surface



- Open-ended W/G source port
- Flann SGH (40 x 30 mm aperture) used on test-port to improve dynamic range (about 25dB with averaging).
- Separation between source W/G and horn aperture = 343mm
- Source- lens distance which gave maximum coupling was assumed to equal focal length.
- Beam waist diameter measured at 150mm distance from lens surface, using open-ended WG.



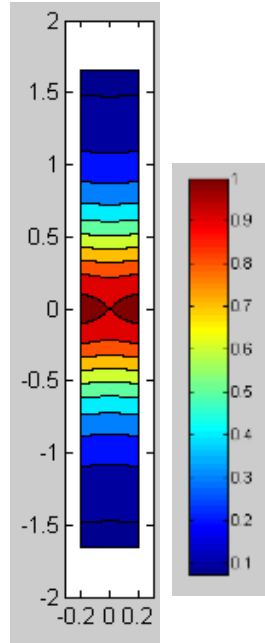
# Initial Measured Results



# GRIN Lens Design using Transformational Optics (TO)

Use of conformal mapping to derive a suitable mapping from convex lens shape to cylinder

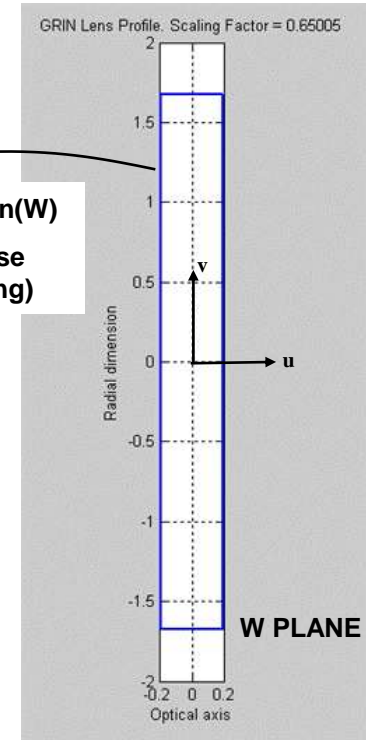
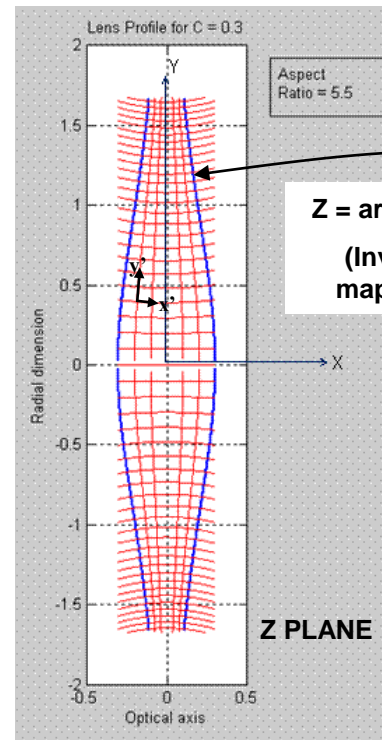
Required  $\epsilon_r$  distribution in equivalent GRIN lens (normalised)



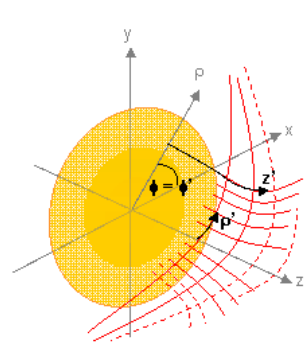
TO equations (J = Jacobean of the mapping):-

$$\mu' = (J \mu J^T) / \text{Det}(J)$$

$$\epsilon' = (J \epsilon J^T) / \text{Det}(J)$$



$Z = \arcsin(W)$   
(Inverse mapping)



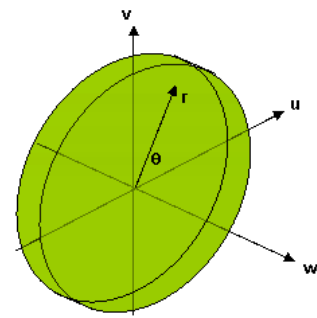
3D mapping

$$r = \cos(z) \sinh(\rho)$$

$$\theta = \phi$$

$$w = \sin(z) \cosh(\rho)$$

Extension to 3D



CO-DOMAIN (cylindrical GRIN lens)

2D Version

# Summary and Proposed Further Work

- The prototype MTM lens performance has yet to be fully characterised, but appears to have:
  - The correct focal length
  - Reasonably low loss
  - Around 10% bandwidth
- Etching misalignment error is up to  $\sim 25\mu\text{m}$  on double-sided lens substrate layers. Worst-case dimensional error is  $\sim 4\%$ . Effect on lens performance is under assessment.
- A GRIN lens design has been derived analytically using a combination of Transformation Optics and conformal mapping. Awaiting ZEMAX modelling.
- Performance of lens with single-side lens substrate layers remains to be measured.
- Further lens measurements planned: (a) repeat of insertion loss (b) surface reflection level (c) aperture field probing
- **FURTHER WORK:**
  - Design and integration of lens matching layers (if required)
  - Rework of lens design to optimise performance
  - The design of Transformation Optics software to assist with GRIN lens design for specialized applications

# Achievements against goals

The programme has achieved the following so far:

- Investigated Design methodologies for GRIN lens including Transformational Optics
- Designed a GRIN lens at 50 GHz using constructed metamaterials
- Manufactured a metamaterial lens using PCB multilayer technology
- Tested the lens at STFC- RAL using Quasi-Optical bench
  - performed in the context the of the TSB BB MWS Radiometer work (Astrium / RAL 2012)
- Zemax analysis of the QO Test System (further zemax modelling to be performed)

## Major issues resolved

- Programmatic
  - Personnel loading at Astrium and RAL due to support to:
    - MWS Phase a study and Phase B Bid
    - TSB MWS radiometer breadboard work
    - Overload on QO test facilities at RAL (MWS D1 dichroic work)
- Design, Manufacture and Test
  - PCB manufacturing accuracy for metamaterial laminates
- Any unresolved issues:
  - There is always more to do !

# Positioning achieved

- Presentations and Publications
  - Poster Paper CEOI Workshop Nottingham Sept 2012
  - Paper presented at the CEOI Training Workshop at RAL on Quasi-Optical Design (Nov 2012)
  - Poster Paper provided at the CEOI Innovations in Remote Sensing Event in London on Metamaterials and QO components (Jan 2013)
- Patents
  - None specific to AGLeD yet !
  - *But ...US patent for MM-wave QO Beam Splitter (Straw Cutter, CEOI Project 2007) – Graham Maxwell-Cox – March 2013 - At Last!*
- Leverage achieved
  - UK QO design capability in lenses for mm-wave radiometer (Applicable to MetOp MWS Radiometer)
- Collaborations forged
  - TSB BB Team for MWS Radiometer (MetOp)
  - STFC RAL MM-wave Test Facilities and Measurement Team
  - MetOp MWS Radiometer Systems team

# Other Achievements

- Training and knowledge exchange
  - 6 months Support to Queens University London from previous CEOI Metamaterial study (Astrium QMUL) to March 2013
- UK Capability enhancement  
Benefits to UK Space
  - Design and test capability in **advanced lens design** for mm-and sub-mm-wave applications
  - Development of **practical metamaterial systems**
  - Development of **Non-sequential Ray Tracing** techniques for QO design and analysis

# Roadmap

- Missions/exploitation route
    - MetOp MWS Radiometer (awarded Astrium UK 2013)
    - Risk mitigation for lens coupled QO systems (53 and 89 GHz)
    - QO modelling of radiometer systems using non-sequential ray tracing
  
  - Future steps
    - Technology development required
  - Design and integration of lens matching layers
  - Rework of lens design to optimise performance
  - Further QO testing required developing measurement techniques
  - The design of Transformation Optics software to assist with GRIN lens design for specialized applications
    - Issues to be resolved
- Manufacturing techniques for scaling to shorter wavelengths